

Key**7-1 Properties of Parallelograms**

A pantograph is used to copy drawings. Its legs form a parallelogram. In $\square JKLM$, $LM = 17 \text{ cm}$, $KN = 13.5 \text{ cm}$, and $m\angle KJM = 102^\circ$. Find each measure.

1. $KM = 27 \text{ cm}$

2. $KJ = 17 \text{ cm}$

3. $MN = 13.5 \text{ cm}$

4. $m\angle JKL = 78^\circ$

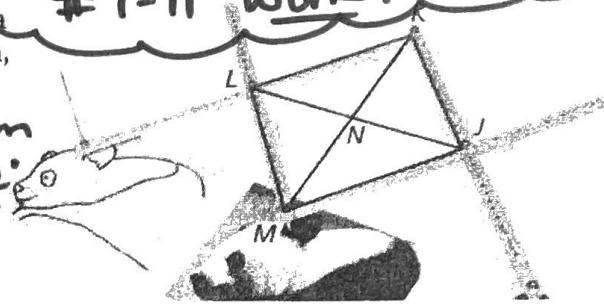
5. $m\angle JML = 78^\circ$

6. $m\angle KLM = 102^\circ$

7. Three vertices of $\square ABCD$ are $A(-3, 1)$, $B(5, 7)$, and $C(6, 2)$. Find the coordinates of vertex D .

$(-2, -4)$

*Check blog video for
1-11 work.



$WXYZ$ is a parallelogram.

Find each measure.

8. $WX = 11$

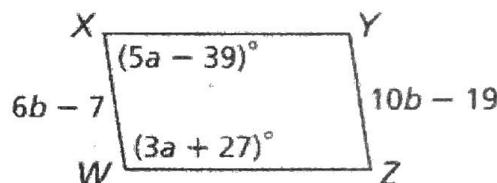
9. $YZ = 11$

10. $m\angle X =$

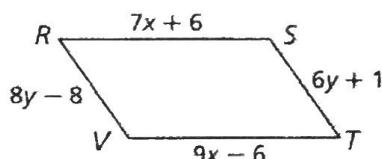
81°

11. $m\angle W =$

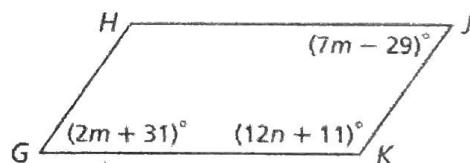
99°



12. Show that $RSTV$ is a parallelogram for $x = 6$ and $y = 4.5$.



13. Show that $GHJK$ is a parallelogram for $m = 12$ and $n = 9.5$.



*See blog video for # 12 & 13.

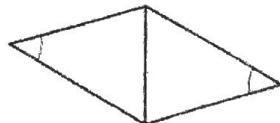
Determine if each quadrilateral must be a parallelogram. Justify your answer.

14.



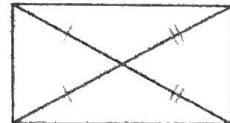
yes

15.



NO

16.



NO

check blog video for work

The flag of Jamaica is a rectangle with stripes along the diagonals. In rectangle $QRST$, $QS = 80.5$, and $RS = 36$. Find each length.

18. SP

$$40.25$$

19. QT

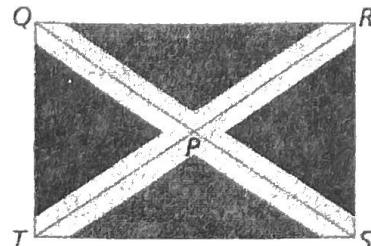
$$36$$

20. TR

$$80.5$$

21. TP

$$40.25$$



$GHJK$ is a rhombus. Find each measure.

22. HJ

$$25$$

23. $m\angle HJG$ and $m\angle GHJ$ if $m\angle JLH = (4b - 6)^\circ$

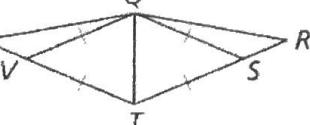
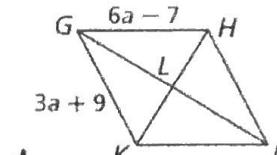
and $m\angle JKH = (2b + 11)^\circ$

$$m\angle HJG = 31^\circ$$

$$m\angle GHJ = 118^\circ$$

24. Given: $QSTV$ is a rhombus. $\overline{PT} \cong \overline{RT}$

Prove: $\overline{PQ} \cong \overline{RQ}$

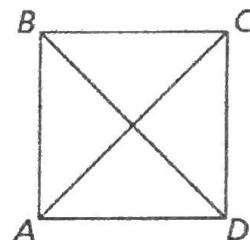


*see video on
blog.

Determine if the conclusion is valid. If not, tell what additional information is needed to make it valid.

25. Given: $\overline{AC} \perp \overline{BD}$ Not Valid

Conclusion: $ABCD$ is a rhombus.



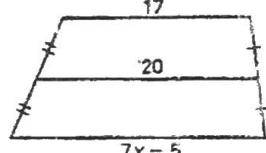
26. Given: $\overline{AB} \cong \overline{CD}$, $\overline{AC} \cong \overline{BD}$, $\overline{AB} \parallel \overline{CD}$

Conclusion: $ABCD$ is a rectangle.

Valid

Find the value of x :

20.

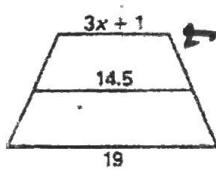


$$\frac{17+7x-5}{2} = 20 \cdot 2 \quad 12+7x=40$$

$$-12 \quad -12$$

$$\frac{7x=28}{x=4}$$

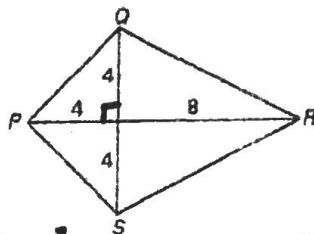
21.



$$\begin{aligned} 3x+1+19 &= 14.5 \cdot 2 \\ 2 & \\ 3x+20 &= 29 \\ -20 & -20 \\ 3x &= 9 \\ x &= 3 \end{aligned}$$

Use the Pythagorean Theorem to find the side lengths of the kite:

17.



$$4^2 + 4^2 = c^2$$

$$16 + 16 = c^2$$

$$\sqrt{32} = \sqrt{c^2}$$

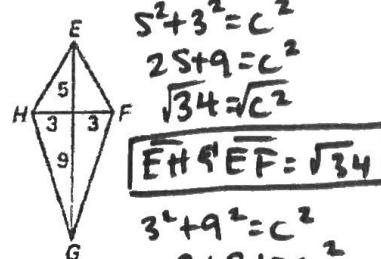
$$4^2 + 8^2 = c^2$$

$$16 + 64 = c^2$$

$$PQ \cong PS: \quad \sqrt{32} = 4\sqrt{2}$$

$$80 = c^2 \quad \sqrt{80}$$

18.



$$5^2 + 3^2 = c^2$$

$$25 + 9 = c^2$$

$$\sqrt{34} = c$$

$$EH \cong EF: \quad \sqrt{34} = \sqrt{34}$$

$$3^2 + 9^2 = c^2$$

$$9 + 81 = c^2$$

$$\sqrt{90} = c$$

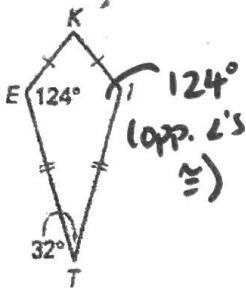
$$\sqrt{90} = c$$

$$QR \cong RS: \quad \sqrt{80} = 4\sqrt{5}$$

$$80 = c^2 \quad \sqrt{80}$$

Find the measure of angle K:

13.

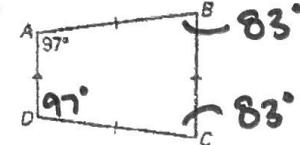


$$360 - 124 - 124 - 32 =$$

$$m\angle K = 80^\circ$$

Find the measure of angle A, B, & C:

4.



$$180 - 97 = 83$$