

Angle of Elevation:

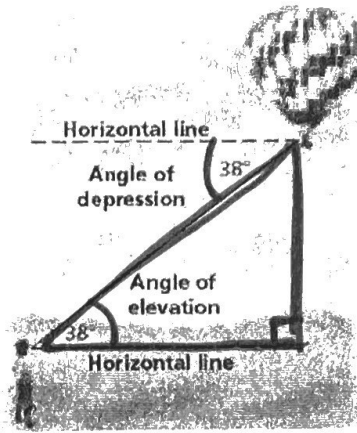
Person on the ground looks up at an object

(inside Δ)

Angle of Depression:

Person looks down at an object

(outside Δ)

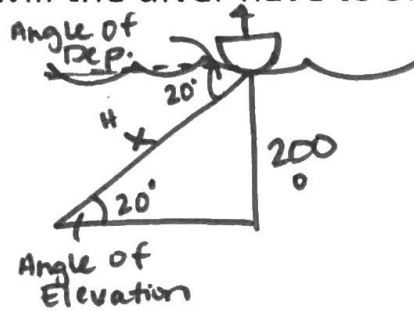


Why are the two angles congruent?

Transversal and parallel lines (alternate interior angles)

Example 1:

A person on a boat on the water spots a sunken treasure that is 200 feet below the water. He jumps out and swims directly to the treasure at an angle of 20° . How far will the diver have to swim to get to the treasure?

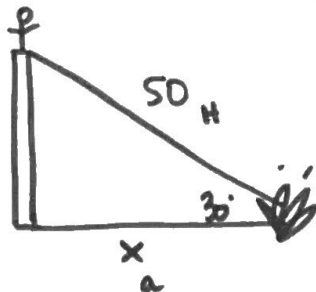


$$\sin 20 = \frac{200}{x}$$

$$\frac{200}{\sin 20} = \boxed{584.76 \text{ ft}}$$

Example 2:

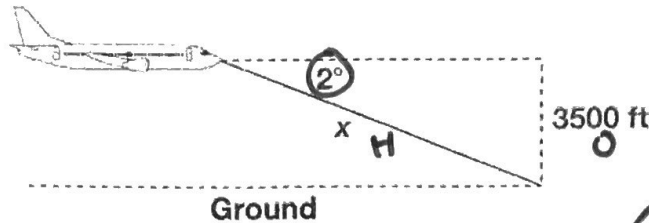
A man standing on a tower spots a fire that is 50 feet from his line of sight at the top of the tower. From the fire, there is an angle of 30° to the top of the tower. How far is the fire from the base of the tower?



$$\cos 30 = \frac{x}{50}$$

$$50 \cos 30 = 25\sqrt{3} = \boxed{43.30 \text{ ft}}$$

Example 3: An airplane flying 3500 ft above ground begins a 2° descent to land at an airport. How many miles from the airport is the airplane when it starts its descent?



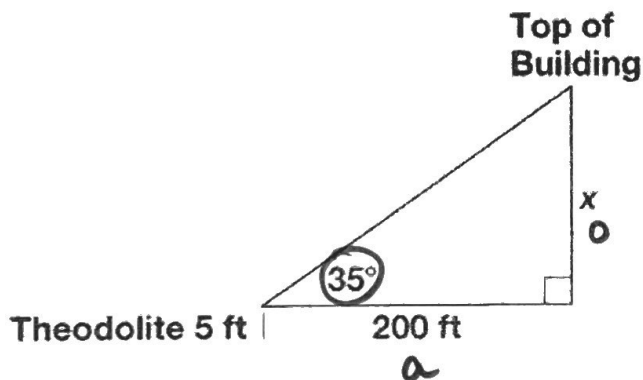
$$\sin 2 = \frac{3500}{x}$$

$$x = \frac{3500}{\sin 2}$$

$$= \frac{100,287.98 \text{ ft}}{5,280} = \boxed{18.99 \text{ mi}}$$

convert to miles

Example 4: A surveyor stands 200 ft from a building to measure its height with a 5-ft tall theodolite. The angle of elevation to the top of the building is 35° . How tall is the building?



$$\tan 35 = \frac{x}{200}$$

$$200 \tan 35 = 140.04 + 5 = \boxed{145.04 \text{ ft}}$$

was measured 5 ft off ground, so have to add back in!